Building Embedded Systems with Embedded DSLs

(Experience Report)

Patrick C. Hickey  Lee Pike  Trevor Elliott  James Bielman  John Launchbury
Galois, Inc.
{pat, leepike, trevor, jamesjb, john}@galois.com

Abstract
We report on our experiences in synthesizing a fully-featured autopilot from embedded domain-specific languages (EDSLs) hosted in Haskell. The autopilot is approximately 50k lines of C code generated from 10k lines of EDSL code and includes control laws, mode logic, encrypted communications system, and device drivers. The autopilot was built in less than two engineer years. This is the story of how EDSLs provided the productivity and safety gains to do large-scale low-level embedded programming and lessons we learned in doing so.

Categories and Subject Descriptors D.3.2 [Language Classifications]: Applicative (functional) languages

Keywords Embedded Domain Specific Languages; Embedded Systems

1. Introduction
Embedded programming involves the lowest levels of abstraction. Most development is in low-level languages, like C or assembly, and programs interact intimately with the hardware. Embedded domain-specific languages (EDSLs) are in some sense at the other end of the software spectrum: they are often embedded (in a different sense of the word!) in high-level programming languages such as Haskell or ML, and are used to lift the programmer’s abstraction level.

That said, there is no reason in-principle why EDSLs cannot be used for embedded programming; this report is about our experience in building new EDSLs for embedded programming and the benefits and difficulties in using them. Our experiences are based on building an autopilot system called SMACCMPilot using our EDSLs. The breadth and scope of the project sets it apart. The audience includes both researchers developing new EDSLs for low-level programming as well as practitioners considering using EDSLs.

Our goal in this paper is to summarize some of our lessons-learned. While we use specific examples, the lessons apply more generally to large embedded-system design in EDSLs. Our target audience includes both researchers developing new EDSLs for low-level programming as well as practitioners considering using EDSLs.

All of the EDSLs described herein, as well as SMACCMPilot itself, are open-source software. Further documentation and links to the sources are available at smaccmpilot.org.

2. Ivory: Safe C Programming
At face value, our approach sounds audacious if not ludicrous: faced with a deadline for developing a new high-assurance autopilot system in one-and-a-half years, start by designing a new programming language and compiler from the ground up.

Of course, developing an EDSL is not the same as developing a stand-alone compiler. Much of the typical compiler tool-chain, such as the front-end parser/lexer, is provided for free by the host language. It took approximately 6 engineer-months to create the first EDSL language and compiler, which totals about 6k lines of Haskell code.

The language we developed for generating safe embedded C code is called Ivory. Ivory compiles to restricted C code suitable for embedded programming. Ivory shares the goal of other “safe-C” languages and compilers like Cyclone [9] and Rust [16]. Our main motivation for not using those languages is our desire for an EDSL providing convenient, Turing-complete, type-safe macro-language (Haskell) to improve our productivity.

There have also been some “safe-C” EDSLs including Atom [8], Copilot [13], and Feldspar [2]. The most significant difference between these languages and Ivory is that they are focused on pure computations (e.g., Feldspar is a DSL for digital signal processing), and do not provide convenient support for defining in-memory data-structures and manipulating memory. Ivory is designed to be a EDSL that can be used for writing safe memory-manipulating embedded C.

Ivory also makes contributions from a programming language perspective, namely in its expressiveness and type-safety. We overview each, then present a small example, to give the reader a feel for the language.

Expressiveness Regarding the expressiveness, Ivory has a variety of useful features, including:

• Memory-areas: the ability to allocate stack-based memory and manipulate both local and global memory areas [4].

Permission to make digital or hard copies of part or all of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. Copyrights for third-party components of this work must be honored. For all other uses, contact the owner/author(s). Copyright is held by the author/owner(s).

ICFP ’14, September 1–6, 2014, Gothenburg, Sweden.
ACM 978-1-4503-2873-9/14/09.
http://dx.doi.org/10.1145/2628136.2628146
• *Product types*: C structs with well-typed accessors.
• *FFI*: typed interfaces for calling arbitrary C functions.
• *Bit-fields*: support for typed manipulation of bit-fields and registers [5].

We built Ivory with some limitations to simplify generating safe C programs. Ivory does not support heap-based dynamic memory allocation (but global variables can be defined). C arrays are fixed-length. There is no pointer arithmetic. Pointers are non-nulable. Union types are not supported. Unsafe casts are not supported: casts must be to a strictly more expressive type (e.g., from an unsigned 8-bit integer to an unsigned 16-bit integer) or a default value must be provided for when the cast is not valid. The most common unsafe C cast is not possible: no void-pointer type exists in Ivory.

In Ivory, these have not been limiting factors, particularly because of the power of using Haskell as a macro system. For example, while array sizes must be of fixed size at C compile-time, we can define a single Haskell function that is polymorphic in the array size that becomes instantiated at a particular size at each use site.

**Type-checking** Ivory’s domain-specific type checking focuses on guaranteeing memory safety and helping programmers reason about their programs’ nonfunctional behaviors more easily.

In addition, Ivory programs have an *effects* type associated with them, implemented as a parameter to the Ivory monad. There are three kinds of effects tracked:

- **Allocation effects**: whether a program performs (stack-based) memory allocation as well as whether pointers point into global or stack memory.
- **Return effects**: whether a program contains a return statement.
- **Break effects**: whether a program contains a break statement.

Allocation effects allow memory allocation to be restricted and tracked at the type level. For example, from a program’s type alone, we can determine whether it allocates memory on the stack, making stack usage easier to track. More importantly for memory-safety, allocation effects also ensure Ivory programs contain no dangling pointers: it is a type error to return a pointer to locally-allocated memory.

Return and break statements fundamentally affect control-flow and can result in unexpected behavior by breaking out of the current block or returning from a function. For example, in a top-level while loop implementing an real-time operating system task, there should be no break or return statements; we can enforce this with the type system. Tracking these effects is novel, we believe, and particularly important in the context of an EDSL in which programs are generated and manipulated heavily in the host language.

In an EDSL, we have at least two options for type checking: (1) write a domain-specific type-checker in Haskell (relying on Haskell’s type-system just for macro-language type-checking), or (2) embed the domain-specific type checker into Haskell’s type system.

We were motivated to pursue option (2) because it allows us to discover problems sooner in the development cycle. In the case of option (1), we only find out about problems in the program’s AST during code generation. Option (2) ensures that all macro and library code is typed correctly, independent of its use in the generated code. We discuss the issues of finding errors early on in more detail in Section 5.

When we began developing Ivory, our hypothesis was that recent type-system extensions to the Glasgow Haskell Compiler (GHC) make it feasible to embed the invariants necessary to ensure memory-safe C programming into the type-system [12]. From a practical standpoint, Ivory demonstrates just how far the type-system has come, allowing us to replicate the type safety of compilers like Cyclone, etc.

We do not have space to adequately describe Ivory’s type-system; we leave that to a forthcoming paper. Here we will note that the embedding depends on the use of data kinds [20], type families [18], and rank-2 polymorphism [10].

**Ivory example** We present a small example of Ivory code. The example omits many features of the language, but should give the reader a feeling for it.

Consider Figure 1, in which an Ivory program is shown, as well as the corresponding generated C sources and headers (making a few syntactic changes to the C for readability, not relevant to the example).

First, we define a struct (or product type) using a quasiquoter that is part of the Ivory language. The Ivory code generated by Template Haskell [19] constructs a struct definition containing two fields consisting of an unsigned byte and an array of 10 signed 16-bit integers. Template Haskell also constructs a new type-level literal, *fooStruct*, that is unique to the defined struct. The *Stored* type constructor signifies that the value is allocated in-memory [4]. The *Array* type constructor takes a type-level natural number as a parameter (available as a Glasgow Haskell Compiler extension) to fix the size of an array.

A procedure, corresponding to a C function, has a type of the form

```haskell
Def (params ::> out)
```

where *params* are the procedure’s parameter types and *out* is its return type. The procedure *setBaz* takes two arguments and its return type is unit, corresponding to the *void* type in C. The types of the procedure’s arguments are types in a type-level list; the first argument is a *reference*, a non-null pointer by construction, to a struct, and the second argument is a signed 16-bit integer. The *Ref* type constructor takes a *scope* type and a memory-area type.
The scope type denotes either stack-allocated scope, or global (and statically allocated) scope. In the example, we expect the reference to be a global.

Procedures are defined with the \texttt{proc} operator that takes a string, corresponding to the name of the function that will be generated in C, and a function from the procedures arguments to its body. The body of the function is an Ivory program that sets each element in the \texttt{baz} field of the struct with the value \texttt{val} passed to it, leaving the \texttt{bar} field unchanged.

Following [4], Ivory guarantees memory-safe array access in the type system since array lengths are statically known. Ivory provides an \texttt{arrayMap} operator that applies a function to each valid index into the array. The function applied in this case is a \texttt{store} operation that takes a reference to a memory area, a value, and stores the value in the area. It is a type-error if the value's type and memory-area's type do not match.

The operation (\texttt{ref -> baz}) takes the struct reference and returns a reference to the \texttt{baz} field. The bang (!) operator takes a reference to an array, an index, and returns a reference to the value at that index. The safety of indexing is maintained since the operator has the type

\begin{verbatim}
(!) :: Ref s (Array len area) -> Ix len -> Ref s area
\end{verbatim}

tying the length of the array to the maximum index. For example, an index type (\texttt{Ix 10}) supports index values from 0 to 9.

The example only shows a small part of Ivory's language and does not exhibit some of its additional features to prevent unsafe programs. For example, if \texttt{set Baz} had allocated stack memory and created a reference to it, then tried to return the reference (creating a dangling pointer), it would result in a type error.

Additionally, for application-specific properties that cannot be type-checked, Ivory permits the insertion of assertions, assumptions on arguments, and requirements on return values. Ivory also automatically inserts checks for arithmetic underflow/overflow and division-by-zero. All these checks are useful during testing and we have used them to assist with static analysis and model-checking the generated C.

3. Tower: from Functions to Architectures

In many embedded systems, programmers produce an entire system of software that interacts with multiple input and output peripherals concurrently using a real-time operating system (RTOS). Typical RTOSes provide just a few low-level locking and signaling primitives for scheduling. Since microcontrollers do not have the virtual memory management units (MMUs) found on larger processors, the RTOS kernel cannot protect any system memory against badly behaved user code. These restrictions put significant burden on programmers: they must ensure all tasks, and all communication between tasks, are implemented correctly.

During our initial development of SMACCMPilot, we found ourselves generating high-quality C functions from Ivory, which guarantees memory-safety of the generated code. But whenever we needed “glue code” to implement inter-process communication, initialize data-structures, read the system clock, lock the processor, etc., we were forced to abandon our well-typed world and tediously use C directly via Ivory’s foreign function interface. Furthermore, the hand-written C is OS-specific, meaning it would have to be rewritten for any OS port.

\textbf{Extending Ivory} The hand-written glue code was ruining both our productivity and our assurance story. We wanted a language to describe the structure of the glue code that would generate it for us. Our key insight was that such an EDSL could be built as a macro over Ivory, using Ivory's code-generation facilities, without losing anything.

From these ideas, the Tower EDSL was born. Tower is an extension to the Ivory language that is designed to deal with the specific concerns of multithreaded software architectures. Tower still allows the programmer to use all the low-level power of Ivory for general programming, but uses a separate language for describing tasks and the connections between them. It took about 4 engineer-months and 3k lines of Haskell code to build Tower. This is one of the great productivity features of working with EDSLs: if we discover the language we built is difficult, tricky, or unsafe for solving a particular problem, we can extend that language with a library without modifying the compiler.

In Tower, one specifies tasks and communication channels, and the Tower compiler generates correct Ivory implementations, as well as architecture description artifacts. Tower hides the dangerous low-level scheduling primitives from the user, and keeps type information for channels (i.e., the datatype of the channel message), expressed as Ivory types, in the Haskell type system.

Tower allows the programmer to describe a static graph of channels and tasks. For the intended use case in high assurance systems, a static configuration of channels and tasks simplifies reasoning about memory requirements and permits the system to be analyzed for schedulability.

\textbf{Multiple interpreters} In the Tower front end, the programmer specifies a system that can be compiled to multiple artifacts.

Tower is designed to support different operating systems via a swappable backend. Since all code that touches operating system primitives is generated by Tower, it is easy for the user to specify a system and compile it for different operating systems. Tower supports both the open-source FreeRTOS [7] as well as the formally verified eChronos RTOS [6] developed by NICTA.

Tower also has a backend which generates a system description in the Architecture Analysis and Design Language (AADL) [17]. We also built a backend for the Graphviz language to generate graphs of tasks and channels. These output formats make it possible to visualize, analyze, and automatically check properties about the system.

\textbf{Tower example} In Figure 2, we sketch a small Tower example that is representative of a device driver that blinks an LED. Small simplifications to Tower have been made in the code, eliding details relating to code generation and backend selection.

In the first column of the figure, the communication architecture is defined in the \texttt{Tower} monad. The program initializes a unidirectional channel between two tasks as well as the tasks themselves. A channel, or queue, consists of transmit (\texttt{tx}) and receive (\texttt{rx}) endpoints, respectively. The \texttt{blinkTask} task is an RTOS task that will send output to the \texttt{lightswitch} RTOS task via an RTOS-mediated channel. The \texttt{lightswitch} task toggles the LED based on the incoming Boolean values. (In the third column, a graph of the tower program is shown, generated from the Tower compiler’s Graphviz dot output, showing the architectural structure of the two tasks as well as the queue between them.)

To conserve space, we only define \texttt{blinkTask}. The second column contains the definition of \texttt{blinkTask}, defined in the \texttt{Task} monad. The \texttt{blinkTask} task takes a channel source and returns a task. The task first initializes an \texttt{emitter} for the channel then creates a reference to allocated memory that is private to the task. Every 100 milliseconds, an Ivy action is taken. In this case, the action is to call Ivy function \texttt{blinkFromTime} that is executed whenever the task is enabled (we elide the implementation of \texttt{blinkFromTime} in this example). The boolean value \texttt{res} is then emitted on the channel.
4. SMACCMPilot: a High-Assurance Autopilot

Our main use for Ivory and Tower thus far has been in building a robust autopilot. The result is SMACCMPilot, an open-source (BSD licensed) autopilot system for quadcopter unmanned air vehicles (UAVs). It is a complete embedded system that includes low-level IO peripheral drivers, an encrypted communication protocol stack, and several layers of control systems.

SMACCMPilot runs on open source flight controller hardware from the PX4 Autopilot project [15]. The hardware platform is a custom printed circuit board with an ARM Cortex M4 microcontroller and the accelerometer, magnetometer, gyroscope, and barometer sensors used to determine the orientation and altitude of the vehicle.

A simplified software architecture of SMACCMPilot is shown in Figure 3. The flight control software is primarily responsible for reading the sensors, estimating the vehicle’s attitude and position using sensor fusion, calculating control outputs, and sending motor power commands to the motor controllers. Higher level controllers manage navigation, and an encrypted command, control, and telemetry link interprets ground station instructions and sends system state to the operator.

The result is a reasonably complex piece of embedded software. SMACCMPilot has 30 tasks connected by 47 channels, and 57 globally shared state variables. Most of those shared state variables are controller tuning parameters, which can be modified by commands sent over the telemetry link.

SMACCMPilot was developed alongside the Ivory/Tower tools. The complete system took approximately 22 engineer-months to develop. The low level drivers for the system were written first in C, then transliterated to Ivory as the language became mature enough to support them. We built a stack for command, control, and telemetry, encapsulated in an encrypted packet protocol. A few components from the ArduPilot open source project, the biggest of which is a 10kloc C++ library for inertial sensor fusion, are still used inside SMACCMPilot. We plan to replace the remaining C++ code with Ivory implementations in the future.

Complexity comparison

The SMACCMPilot application code is 10kloc of Ivory, the board support code is 3kloc of Ivory (and Tower), and the telemetry link binary packing and unpacking code is a machine-generated 10kloc of Ivory code. When compiled, the complete application is 48kloc of generated C code, and depends on some external C libraries to implement the operating system (4kloc) and other functions, such as sensor fusion. This is comparable to existing open source flight controller systems.

We can compare this to two systems which have a similar feature set and run on similar hardware to SMACCMPilot. The ArduPilot project [1] and the PX4 project are popular open source autopilots. Both implement all of the low level drivers to support similar (or identical) microcontroller based flight controller boards, comparable control laws, and implement the same MAVLink telemetry protocol. We do note that the APM and PX4 projects have more high level autonomous capabilities than SMACCMPilot has at this time.

The ArduPilot project is over 60kloc of C++, runs in three pseudo-threads, and supports at least four distinct autopilot hardware platforms. The PX4 Autopilot software stack has 25kloc of C/C++ application code, 25kloc of C/C++ platform support code, and depends on the large (50kloc+) NuttX operating system.

5. Lessons Learned

In this section, we discuss some of the benefits and challenges of using EDSLs for embedded programming, focusing on those that were surprising to us, despite our teams’ previous experience in functional programming and embedded development.

Our experience using Ivory and Tower to build SMACCMPilot has been an extreme lesson in “eating our own dog-food”. We had multiple developers writing the compilers and using them to build applications concurrently. We learned a few less that are relevant to any compiler development but particularly relevant to EDSL development.

Type-checking for embedded programming

Build times are non-trivial for large software systems. At the time of writing, a fresh build of SMACCMPilot and associated test programs is over seven minutes of real time (and 12 minutes of CPU time since we have a multi-threaded build system). One reason the build time is so large is that it requires Cabal (the Haskell package manager) to discover library dependencies and install packages, compile the Haskell sources, and then compile the C sources. As well, some sources are compiled multiple times for different targets on multiple operating systems.

Figure 3. Simplified diagram of SMACCMPilot software architecture. Tasks written in Ivory are shown as white boxes, tasks implemented in legacy C++ code are gray boxes, channels are arrows, hardware components are black boxes.

Figure 2. Tower (Col. 2), Task (Column. 1), Graphviz output (Col. 3)
Then, to execute the software on the embedded device, we have to write the software to the device’s memory via a JTAG programmer or a serial bootloader, which takes on the order of ten seconds.

All this is to say that the end-to-end debug cycle might mean testing a small number of changes to Ivory or Tower per hour. Clearly, the debug cycle in embedded development particularly motivates us to make fewer bugs and to discover them early.

During development, it became apparent how useful Haskell type-checking is for embedded programming. As described in Section 2, we have embedded Ivory’s type system in Haskell’s. Thus, domain-specific type-errors are caught during Haskell type-checking. Type-checking, and other static warnings reported by GHC, are nearly instantaneous since it can be done on a module-by-module basis. The type system tracks the global or stack frame provenance of references, as well as structure accessors and array indices, to ensure all well-typed Ivory programs generate memory-safe C.

The upshot is that Ivory programs that would generate unsafe C programs are caught immediately.

In addition, we have found it useful to detect potential bugs even if the C compiler might also detect them. To take one example, consider unused variable declarations. While a C compiler can detect this, perhaps late in the compilation phase, we discover these warnings nearly instantaneously during type checking. Moreover, the more preprocessing we can do in Haskell, the more potential errors we may find, and with a better relation to the EDSL source.

However, not every property of interest in embedded programming can be conveniently embedded in the Haskell type system with GHC extensions. For example, integer overflows checks are not practical to embed. Moreover, GHC’s type error reporting can be unwieldy. Ivory users would benefit from domain-specific error reporting which could, for example, describe type errors in the vocabulary of Ivory, rather than burden the user to interpret the way the Ivory language types are embedded into Haskell types. For example, passing the wrong number of arguments to an Ivory function in a procedure call is reported as a type error when using functional dependencies, whereas a mismatch between the type of a procedure and the number of arguments provided in its declaration is reported as a kind error. The errors reported are of the particular type-level implementation given for Ivory types. Haskell does not yet have good facilities for type-level programming abstraction.

**Type-safe system plumbing** Adding many new features to SMAC-CMPilot is easy. In fact, the most tedious part is writing the business logic in Tower, where we define a new task, and then plumbing values representing communication channels through the code. There is nothing conceptually difficult in doing so—it is similar to any monadic interface for specifying a graph. When changes cross Haskell function boundaries, we must modify the arguments to the Haskell function that generates the Tower task (or modifying the fields of a data-type if channels have been grouped together). Channels are typed, so type-checking detects most plausible inter-task communication errors.

Stepping back, the idea that plumbing arguments to Haskell functions is the hardest part of embedded development is amazing. We are not dealing with bugs in low-level OS interfaces, we are not making timing or resource contention errors in communication, and we are not dealing with type-errors like you might find in raw C (where data might be cast to `void*` or `char[]`).

Because plumbing is so easy, it encourages us to improve modularity in the system. Defining a new RTOS task is easy, so we might as well modularize functionality to improve isolation and security. For example, in the ground station communication subsystem, encryption and decryption are each executed in isolated tasks, simplifying the architectural analysis of the system. As we noted in Section 4, our system is significantly more modular than other autopilots.

**Faking a module system** In Ivory and Tower, top-level functions and structures are packaged into a Haskell data structure to provide to the Ivory compiler. The onus is on the programmer to package up all the necessary components.

On one hand, the approach provides the programmer control over how to modularize the generated C code, deciding which definitions to put in a C source or header file. On the other hand, we have found it to be verbose, tedious, and error-prone. Generally, we want the C files to have similar structure to the Haskell modules in which Ivory programs are written. From that respect, the Ivory module system simply duplicates the Haskell module system.

Worse is when the programmer forgets to package a definition. The error only becomes apparent at C link time, near the end of a long build process. Missing definitions have plagued our builds.

We could move symbol resolution up the build cycle to the C-code generation phase. Ideally, we would move it up the build cycle even further. We are currently exploring the use of Template Haskell to generate Ivory modules at compile-time to assist the programmer.

**Control your compiler** If we were writing our application in a typical compiled language, even a high-level one, and found a compiler bug, we would perhaps file a bug report with the developers... and wait. If we had access to the sources, we might try making a change, but doing so risks introducing new bugs or at the least, forking the compiler. Most likely, the compiler would not change, and we would either make some ad-hoc work-around or introduce regression tests to make sure that the specific bug found is not hit again. Such a situation is notorious in embedded cross-compilers that usually have a small support team and are themselves many revisions behind the main compiler tool-chain.

But with an EDSL, the situation is different. With a small code-base implementing the compiler, it is easy to write new passes or inspect passes for errors. Rebuilding the compiler takes seconds.

More generally, we have a different mindset programming in an EDSL: if a class of bug occurs a few times—whether caused in the compiler or not—we change the language/compiler to eliminate it (or at least to automatically insert assertions to check for it). Instead of a growing test-suite, we have a growing set of checks in the compiler, to help eliminate both our bugs and the bugs in all future Ivory programs.

We claim that Ivory code compiles to memory-safe C code. However, a formal proof of these claims, or more generally, a proof that the semantics of Ivory programs are implemented by the generated C code, is work-in-progress. However, a small number of primitives and simple compiler facilitates inspection and testing. In all, this is less assurance than is given by fully verified toolchains, such as CompCert [11]. Other approaches more specific to bringing assurance to EDSL compilers could be borrowed as well [14].

**Everything is a library** With an EDSL, and particularly a Turing-complete macro language, everything is a library. The distinction between language developers and users becomes ambiguous. As an extreme example, one can think of Tower as “just” a library for Ivory. A small example is defining a conditional operator in terms of Ivory’s if-then-else primitive as shown in Figure 4. All types above were introduced in Section 2. With the `cond_` operator, we can replace nested if-then-else statements as shown in the figure with more convenient conditionals, without modifying the language.

Because macros are so easy to define and natural in EDSL development, our biggest challenge has been ensuring developers on our team put useful ones in a standard library, to be shared.
6. Conclusions

We have described our use of the Ivory and Tower EDSLs for building a large embedded system. Many of the advantages of EDSLs for embedded programming relate to type-checking in Haskell. Of course, some bugs cannot be caught statically. For the most part, once type-checking is complete, we are confident that the bug is a logical bug. We do not spend our time chasing segmentation faults or strange undefined or compiler-dependent behaviors but rather focus on the bugs that result from our misunderstanding of the application, not the programming environment.

What is next? In the next few years, SMACCMPilot will continue to grow. It, along with the Ivory & Tower tools, are open source, in the hope of engaging a broader community. We will add new hardware, new sensors, and new controllers so that it is competitive with others in terms of functionality.

In addition, we are looking to improve the usability of Ivory and Tower. For example, we are working to integrate verification tools more closely into the language. We have also begun to define quasiquoters for the languages so that C programmers might feel more at home with the language but power (Haskell) users can still enjoy the benefits of EDSL programming.

In short, we believe EDSLs can be brought down from the ivory tower (pun intended) to the grungy world of embedded programming.

Acknowledgments

This work is supported by DARPA under contract no. FA8750-12-9-0169. Opinions expressed herein are our own. A number of people have provided input and advice; we particularly thank Kathleen Fisher, Iavor Diatchki, and Andrew Tridgell. Joe Kiniry and Adam Foltzer, and the anonymous reviewers provided helpful comments on earlier drafts of the paper.

References


